ADVANCES IN THE PREDICTION OF PISTON TOP RING
FRICATIONAL BEHAVIOUR

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ABSTRACT:
This paper presents the results of simulations on the energy loss for the friction interaction top ring/cylinder wall in a SI engine taking into account the mixed lubrication (ML) regime and considering different engine operating conditions, lubricant viscosity, surface roughness. The oil film thickness prediction describes a sensible different behavior in the case of the entire stroke in ML regime while the plots confirm bigger portions of the four strokes in hydrodynamic regime for high speed/low load operating conditions. A quite insensible response of the friction coefficient is observed for ring roughness around 1.00 μm, while an effective gain on the mechanical efficiency is achievable only below 0.40 μm.

KEYWORDS:
simulation, engine mechanical efficiency, friction losses, mixed lubrication

1. BRIEF LITERATURE REVIEW

A significant share of the total fuel energy (Figure 1) in a modern automotive engine is dissipated in the friction upper compression ring/cylinder wall friction. On this basis, the lubrication of the piston ring has been an important research matter for many years because it is extensively accepted that the interaction at the ring-cylinder wall interface provides substantial effects on friction, wear, oil consumption and power loss in IC engines, as showed in the papers of Furuhama et. al. [1], Taylor [2] and Takiguchi et al. [3].

The piston rings are basically a set of sliding seals whose purpose is to separate the combustion gases above the piston from the crankcase environment below. The most common arrangement is a set of three rings (Figure 2), the upper compression ring, the lower compression ring and the oil control ring.

The ring-cylinder wall interface is particularly interesting as it has been estimated to account for 20% of the total engine mechanical friction by Ting [4], due to the most severe environment in terms of temperature and load, so much effort has been directed to this particular ring. Because of the piston is during its stroke always in an unsteady state, the frictional behaviour of the rings is very complex.

This paper introduces the results of simulations concerning the friction interaction top ring/cylinder wall of a SI engine, taking into account the mixed lubrication (ML) regime and considering different engine operating conditions, lubricant viscosity, surface roughness.
2. THE MIXED LUBRICATION REGIME FOR THE RING

The implemented mathematical model is based on the sharing of the total load acting in the ring radial direction between the hydrodynamic lubrication (HDL) force and the solid-to-solid interactions along the asperities of the surfaces as approached by Greenwood et al. [5], Gelinck et al. [6] and Senatore et al. [7]:

\[ F_R = F_C + F_H \]  

with \( F_C \) the load carried by the interacting asperities and \( F_H \) the one carried by the hydrodynamic component. The total friction force \( F_f \), acting on the ring in tangential direction, is the sum of the friction force between the asperities and the shear force about the HDL regime:

\[ F_f = \sum_{i=1}^{N_a} \int \int \tau_{C_i} dA_{C_i} + \int \int \tau_{H} dA_{H} \]  

with \( N_a \) the number of asperities in contact, \( A_{C_i} \) the area of contact of a single asperity \( i \); \( \tau_{C_i} \) the shear stress at the asperity contact \( i \); \( A_{H} \) the contact area of the ring in HDL regime and \( \tau_{H} \) the shear stress of this component.

The friction coefficient \( f \) can be calculated by the following equation:

\[ f = \frac{F_f}{F_R} = \frac{F_{f,b} + F_{f,h}}{F_R} = \frac{\sum_{i=1}^{N_a} \int \int \tau_{C_i} dA_{C_i} + \int \int \tau_{H} dA_{H}}{F_R} \]  

Both the components, \( F_C \) and \( F_H \), show a strongly dependence by the height \( h_0 \) of the central point of the piston top ring (barrel shape), i.e., the minimum nominal distance between the ring and the cylinder wall.
2.1. The friction due to the deformation of the asperities

For the direct contact between the surfaces the pressure generated by the deformation of the asperities is taken into account according to [6]:

\[
p_c(x) = \frac{2}{3} n \beta \sigma_s \frac{\sigma_s E' F_{3/2} (h(x))}{\beta}
\]

with \( h(x) \) the separation between the two surfaces, \( n \) the density of the asperities, \( \beta \) the average radius of the asperities and \( \sigma_s \) the standard deviation of the height distribution of the summits.

The function \( F_{3/2} \) is given by the following expression:

\[
F_{3/2}(h) = \int_h^\infty (s-h)^{3/2} \phi(s) \, ds
\]

where, the \( \phi \) function is the standardized height distribution of the summits, assumed given by the Gaussian distribution law (6a); the (6b) allows calculating the radial asperity force:

\[
\phi(s) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2} s^2\right)
\]

\[
F_b = \int_0^L \int_0^L p_c(x) \, dA
\]

2.2. The hydrodynamic lubrication model

The normal load due to the HDL regime and the shear stress due to the film lubricant have been calculated by integrating the Reynolds equation in the one-dimensional form:

\[
\frac{\partial}{\partial x} \left( h^3 \frac{\partial p}{\partial x} \right) = 6\mu U \frac{\partial h}{\partial x} + 12\mu \frac{\partial h}{\partial t}
\]

with the boundary conditions as in [8], with the data about the areas at \( p_1 \), \( p_2 \) and \( p_3 \) (Figure 2), from [9].

The viscous shear stress is described by:

\[
\tau_H(x) = -\mu \frac{U}{h(x)} + \frac{h(x) \, dp}{2 \, dx}
\]

In this research, the lateral drag motion of the entire piston ring due to the approaching secondary-motion of the piston to the cylinder wall has not been considered, while other analysis take into account this phenomenon to analyze the ring flexibility as in D’Agostino et al. [10]. Then the ring distance from the cylinder is evaluated with the axial symmetry assumption and in a quasi-static evolution.

3. SIMULATION ALGORITHM

The data of the Table 1 have been involved in all the simulations about the analysis of the friction behaviour of the considered piston ring. The implemented algorithm calculates the monotonically decreasing function \( F_c \) versus \( h_0 \) with the chosen set of geometrical and material resistance data.

Then, for the instantaneous values of the piston speed \( U \) and the pressure boundary conditions, the Reynolds equation is solved allowing the numerical iterations for the inversion of the (9), in the unknown variable \( h_0 \):

\[
F_c(h_0) + F_H(h_0, U, p_1, p_3) - F_{R,t} - F_{R,g}(p_2) = 0
\]

At each step of the numerical procedure, the crankshaft position \( \theta \) is increased by a defined step (0.010 rad), the \( U \) value is updated as well as the pressure
conditions from the indicated cycle; then, iterations are performed on the HDL and asperities components for satisfying the equilibrium condition with the algebraic constrain given by the total radial load $F_R$, i.e., the sum of the ring tension and the gas pressure acting on the ring back side (9).

The numerical simulations were carried out with the inter-ring gas pressures (see Figure 2) according to [9] and the data in Table 1.

Once the previous equation has solved and the minimum ring distance from the cylinder wall $h_0$ is known, the friction forces and the friction coefficient can be calculated using the relationships above described (2, 3 and 8).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Density of asperities</td>
<td>$n$</td>
<td>$10^{11}$</td>
<td>m$^{-2}$</td>
</tr>
<tr>
<td>Average radius of asperities</td>
<td>$\beta$</td>
<td>10</td>
<td>$\mu$m</td>
</tr>
<tr>
<td>Standard deviation of the asperities</td>
<td>$\sigma_s$</td>
<td>0.20-0.60-1.00*</td>
<td>$\mu$m</td>
</tr>
<tr>
<td>Reduced modulus of elasticity</td>
<td>$E'$</td>
<td>231</td>
<td>GPa</td>
</tr>
<tr>
<td>Length of the top ring</td>
<td>$L_t$</td>
<td>1.50</td>
<td>mm</td>
</tr>
<tr>
<td>Cylinder bore</td>
<td>$B$</td>
<td>76.0</td>
<td>mm</td>
</tr>
<tr>
<td>Oil viscosity</td>
<td>$\mu$</td>
<td>5.0-15.0*-25.0</td>
<td>mPa s</td>
</tr>
<tr>
<td>Maximum pressure of the indicated cycle</td>
<td>$p_{cyl}$</td>
<td>0-10-30</td>
<td>bar</td>
</tr>
<tr>
<td>Engine speed</td>
<td>$N$</td>
<td>1000, 3000, 5000</td>
<td>rpm</td>
</tr>
<tr>
<td>Connecting-rod length</td>
<td>$L_{CR}$</td>
<td>129</td>
<td>mm</td>
</tr>
<tr>
<td>Characteristic ratio of the slider-crank mech.</td>
<td>$L_{CR}/R_c$</td>
<td>3.30</td>
<td>-</td>
</tr>
</tbody>
</table>

*Standard condition unless otherwise specified.

4. RESULTS AND DISCUSSION

4.1. Effect of the radial load

The Figures 3 compare the predicted effects of the radial load to the piston ring on the friction coefficient for an engine speed equal to 3000 rpm.

The plots are presented with the choice of the oil dynamic viscosity as parameter. In an actual engine model, this radial force is the sum of the ring tension and the gas pressure acting in the radial direction (chamber at pressure $p_2$).

Two effects can be observed as immediate upshot:
1) for increasing radial load acting on the back side of the ring due to a bigger pressure in the cylinder, the transition to fully developed HDL regime is delayed during the expansion after the TDC position ($\theta = 2\pi$); this transition occurs at an early crankshaft position $\theta$ for the lubricant with viscosity 25 mPa s;
2) the whole four strokes exhibit interaction in mixed-lubrication conditions for oil viscosity equal to 5 mPa s.
4.2. Effect of the speed

The lubricant film thickness and the load carried by oil pressure increase with increasing running speeds. For this reason, when the engine runs at low speed the existence of high friction coefficients near dead centres, indicating metal-to-metal contact, is extended to a big portion or the entire piston stroke. The Figures 4 and 5 show that for engine speed equal to 3000 and 5000 rpm, the transition to fully developed HDL regime occurs in the first 10% of the stroke path, while a considerable first fraction of the expansion stroke shows evidence of the coexistence of boundary and hydrodynamic lubrication, due to the increased cycle pressure and, then, radial ring load.

As predictable, the higher is the viscosity and the higher the HDL friction force Figure 6(a), while the oil film thickness demonstrates a sensible different behaviour in the case of the entire stroke in mixed lubrication regime, Figure 6(b).

The following two figures illustrate on each plot the HDL friction force in coexistence with the boundary one (dash line) and the part of stroke where the oil film is fully developed (solid line).

The figures confirm bigger portion of stroke in HDL regime for high speed/low load operating conditions.
4.3. Effect of the surface roughness

This analysis on the ML-regime for the piston top confirms a quite insensible behaviour of the friction coefficient for ring roughness in the range 0.60 ÷ 1.00 μm, while an effective gain on the mechanical efficiency is achievable in the range 0.20 ÷ 0.40 μm. This outcome may lead the designers toward a balanced cost-benefit analysis. The Figure 8 proves the significant impact of the surface roughness, in the above mentioned ranges.

4.4. Effect of the oil viscosity

The analysis takes into account the lubricant viscosity in the range 5.0 ÷ 25.0 mPa s, the typical values for the commercial defined 0W30 or 5W30 along the temperature range 70-100°C. For higher viscosity, the lubrication regime is hydrodynamic over most of the stroke, also in presence of the high radial load during the expansion stroke, as shown in the Figure 9, where the boundary friction force declines to zero with the delay of the transition boundary-hydrodynamic regime for the lower viscosity oil up to 80 crankshaft degrees.

The four figures in Figure 10 illustrate the effect of the viscosity on the total friction force acting on the ring at 1000 and 5000 rpm, for a maximum cycle pressure equal to 10 and 30 bar, while the surface roughness is 1.00 μm in all the cases.
The oil with low viscosity exhibits lower friction force for high speed and low radial load, while the high viscosity has better effect on the mechanical efficiency on the opposite side.

![Figure 9: Boundary friction force at 5000 rpm, $p_{cyl} = 10$ bar](image)

![Figure 10(a): Total friction force; 1000 rpm, $p_{cyl} = 10$ bar](image)

![Figure 10(b): Total friction force; 1000 rpm, $p_{cyl} = 30$ bar](image)

![Figure 10(c): Total friction force; 5000 rpm, $p_{cyl} = 10$ bar](image)

![Figure 10(d): Total friction force; 5000 rpm, $p_{cyl} = 30$ bar](image)

Another way to get assessments about the viscosity inference on the friction engine dissipation is the comparison among the instantaneous friction power loss. As underlined by the following figure, the operating condition with high engine speed (5000 rpm) and no-load (open valves) is the limit one when the oil with the minimum viscosity has to be preferred. The figure 12 shows a good behaviour of the other two lubricants for increasing radial loads.
The following plots introduce the friction work in a whole thermodynamic cycle \((4 \pi \text{ rad})\) expressed in the conventional terms of friction mean effective pressure, \(W_f\), divided by the displacement, covering the operating conditions proposed above:

- **low/medium/high speed**: 1000, 3000, 5000 rpm;
- **low/medium/high load**: cylinder pressure (indicated cycle): 0 bar (open valves), 10 bar (motoring), 30 bar (medium/full load).

\[
W_f = \int_{s=0}^{s=2\pi} F_f(s) \, ds = \frac{4\pi}{\omega} \int_0^{4\pi} F_f(\theta) \frac{U(\theta)}{\omega(\theta)} \, d\theta \quad (10)
\]

\[
f_{\text{mep}} = \frac{W_f}{V} = \frac{1}{\pi R^2 (2R_c)} \int_0^{4\pi} F_f(\theta) \frac{U(\theta)}{\omega(\theta)} \, d\theta \quad (11)
\]

The underlined numbers in the Figure 13 identify the lower \(f_{\text{mep}}\) value for the specified load/speed combination.

**Figures 13**: Friction mean effective pressure, \(f_{\text{mep}}\) (bar) oil viscosity
- (a) 5.0 mPa s
- (b) 15.0 mPa s
- (c) 25.0 mPa s
5. CONCLUDING REMARKS

The results of simulations about the friction interaction of the piston upper compression ring of a SI automotive engine taking into account the mixed lubrication regime have been presented.

Lower oil viscosity allows lower friction force for high speed and moderate radial load, while the high viscosity one produces better effect on the mechanical efficiency on the opposite side. This analysis reveals a quite insensible behaviour of the friction coefficient for ring roughness in a wide range in the neighbour of 1.00 μm, while an effective gain on the mechanical efficiency is achievable only declining to the range 0.20-0.40 μm.

The oil film thickness prediction describes a sensible different behaviour in the case of the entire stroke in mixed lubrication regime.

The plots confirm bigger portion of the four strokes in HDL regime for high speed/low load operating conditions. The outcomes show that for engine speed up to 3000 rpm, the transition to fully developed HDL regime occurs in the first 10% of the stroke, while a considerable first fraction of the expansion stroke shows evidence of the coexistence of boundary and hydrodynamic lubrication due to the increased cycle pressure and, then, radial ring load.

The good agreement with the theoretical and experimental results of [9] and [11], allows using this mathematical approach/numerical procedure as an effective tool for predicting the piston rings friction losses in a wide range of engine operating conditions and rings arrangement.

List of symbols

- $A_i$: Area of single asperity contact
- $B$: Cylinder bore
- $E'$: Reduced modulus of elasticity
- $F_C$: Normal load carried by the asperities
- $F_H$: Normal load carried by hydrodynamic comp.
- $F_r$: Ring friction force
- $F_{R,t}$: Ring tension
- $F_{R,g}$: Radial force due to the gas pressure $p_2$
- $F_{3/2}$: Asperities height function
- $h$: Oil film thickness
- $h_0$: Minimum ring distance from cylinder wall
- $L_{CR}$: Connecting-rod length
- $n$: Density of asperities
- $N$: Engine speed (rpm)
- $N_a$: Number of contact asperities
- $p$: Hydrodynamic pressure
- $p_C$: Asperities local contact pressure
- $p_{col}$: Gas pressure from indicated cycle
- $p_i$: Pressure in the areas of Fig. 2
- $R$: Piston radius
- $R_C$: Crankshaft radius
- $U$: Piston axial speed
- $V$: Engine displacement per cylinder
- $x$: Ring/Piston axial coordinate
- $t$: Time
- $\beta$: Average asperities radius
- $\phi$: Standardized height distribution
- $\mu$: Oil dynamic viscosity
- $\sigma_{i}$: Height distribution standard deviation
- $\tau$: Shear stress at the asperity contact
- $\tau_{H}$: Shear stress of the hydrodynamic lubrication
- $\omega$: Engine speed (rad s$^{-1}$)

REFERENCES


